# Chimera-like state in ensemble of bistable neurons

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Abstract—We investigate the nonlinear dynamics of a neural network. As a model of a neuron, we use Hodgkin-Huxley mathematical model. We choose the neuron's parameters corresponding to a bistable region in which both fixed point and limit cycle are coexisting. We discover that depending on external current and coupling strength we can achieve a chimera-like state when one part of the neurons is in the resting state, while the other one is in the oscillatory regime in a certain area of coupling strength and external current amplitude.

*Index Terms*—Complex network, Hodgkin-Huxley neuron, neural network, chimera-like state.

## I. INTRODUCTION

The dynamics of complex networks has attracted much attention in recent years [1]–[6]. Especially, the networks of spiking neurons or neuron-like elements take a significant part of this area [7]–[9]. The interest in neural networks is due it helps to make a contribution to a better understanding of brain functionality, that also is of a grate interest [10]–[15].

Collective dynamics in a neuronal network is usually considered by taking into account that every neuron in the network is monostable, i.e., it has a single stable trajectory [16]. However, according to Keener and Sneyd [17], the Hodgkin-Huxley (HH) model exhibits bistability in a narrow range of control parameters near the excitation threshold. The bistability regime in oscillatory systems as known to be of special interest due to a variety of hidden unexpected phenomena.

We investigate the nonlinear dynamics of a networks of Hodgkin-Huxley neurons for the parameters' values corresponding to a bistable region in which both fixed point and limit cycle are coexisting. We discover a phenomenon when one part of the neurons are in the resting state, while the other one is in the oscillatory regime in a certain area of coupling strength and external current amplitude.

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## II. MODEL

We consider the network of N = 100 Hodgkin-Huxley neurons. The time evolution of the transmembrane potential of the HH neurons is given by [18]

$$C_m \frac{dV_i}{dt} = -g_{Na}^{max} m_i^3 h_i (V_i - V_{Na}) - g_K^{max} n_i^4 (V_i - V_K) - g_L^{max} (V_i - V_L) + I_i^{ex} + I_i^{syn}$$
(1)

where  $C_m = 1\mu F/cm^3$  is the capacity of cell membrane,  $I_i^{ex}$  is an external bias current injected into a neuron in the network,  $V_i$  is the membrane potential of *i*-th neuron, i = 1,...,N,  $g_{Na}^{max} = 120mS/cm^2$ ,  $g_K^{max} = 36mS/cm^2$  and  $g_L^{max} = 0.3mS/cm^2$  receptively denote the maximal sodium, potassium and leakage conductance when all ion channels are open.  $V_{Na} = 50mV$ ,  $V_K = -77mV$  and  $V_L = -54.4mV$  are the reversal potentials for sodium, potassium and leak for sodium, potassium and leak are open sepectively. m, n and h represent the mean ratios of the open gates of the specific ion channels.  $n^4$  and  $m^3h$  are the mean portions of the open potassium and sodium ion channels within a membrane patch. The dynamics of gating variables (x = m, n, h) are given:

$$\frac{dx_i}{dt} = \alpha_{x_i}(V_i)(1 - x_i) - \beta_{x_i}(V_i)x_i, \qquad x = m, n, h \quad (2)$$

 $\alpha_x(V)$  and  $\beta_x(V)$  are rate functions, described in [19].

 $I_i^{syn}$  is the total synaptic current received by neuron *i*. We consider coupling via chemical synapses. The synaptic current takes the form [20]

$$I_i^{syn} = \sum_{j \in neigh(i)} g_c \alpha(t - t_0^j) (E_{rev} - V_i)$$
(3)

where the alpha function  $\alpha(t)$  describes the temporal evolution of the synaptic conductance,  $g_c$  is the maximal conductance of the synaptic channel and  $t_0^j$  is the time at which presynaptic neuron j fires. We suppose  $\alpha(t) = e^{-t/\tau_{syn}}\Theta(t)$ , there  $\Theta(t)$ is the Heaviside step function and  $\tau_{syn} = 3ms$ . The initial conditions of all neurons correspond to the oscillatory basin of attraction of individual neuron.

# III. RESULTS

We investigate the dynamics of network with scale-free topology and analyze how the number of active neurons depends on both external current and coupling strength. By active neurons we mean the ones generating spikes.  $I^e = 6.24$  is the threshold value for a single neuron and for current amplitudes lower that value a neuron can be only in a "silent" regime. On the other hand for big values of external current  $(I^e > 8.0)$  all neurons are in oscillatory regime independently on coupling strength. Between these two threshold values of  $I^e$  networks dynamics depends on  $q_c$ .

We find a specific regime in which one part of neurons is in the resting state while another one generates spikes. We called it chimera-like state. The situation when in a complex network one part of the elements is in the resting state while another one generates spikes is of interest. And it is not so clear why the system behaves this way, because all connections in the network are excitatory, and at the first blush excitatory synapses shouldn't suppress neuron oscillations and external current is above the threshold.

It is known that dynamics of one bistable Hodgkin-Huxley neuron can be switched from oscillatory regime to resting one by short pulse of external current. In that case excitatory synapses can be represented as such pulse. So, in the network of bistable Hodgkin-Huxley neurons they can switch the dynamics of each other and as a result we observe the chimeralike state when we have two parts of neurons with different dynamics.

The excitatory synapses with the big enough amplitude can switch the neuron dynamics from initially being oscillatory to the resting one. So if all neurons in the network oscillate initially, the dynamics of the neurons with a high number of input connections can be easily switched to the resting one, while other ones having a small number of connections continue to generate spikes.

# **IV. CONCLUSION**

We have investigated the nonlinear dynamics of a neural network. As a model of a neuron, we used the Hodgkin-Huxley mathematical model. We have chosen the neuron's parameters corresponding to a bistable region in which both fixed point and limit cycle are coexisting. We have discovered that depending on external current and coupling strength we can achieve a chimera-like state when one part of the neurons is in the resting state, while the other one is in the oscillatory regime in a certain area of coupling strength and external current amplitude.

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