

# Modeling of a brain neuronal network under visual stimulation

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**Abstract**—We numerically simulate a network of coupled Hodgkin-Huxley neurons for modulating a processing visual perception by the brain. On a part of the network, we apply an external current of constant amplitude modulating visual information entering the brain. We analyze the influence of the external stimulus amplitude on the dynamics of the system. We discover coherent resonance phenomenon when for certain area of external stimulus amplitude both signal-to-noise ratio and characteristic correlation time are maximal.

**Keywords**—*Hodgkin-Huxley neuron, neural network, biological neuron, visual stimulus, coherent resonance.*

## I. INTRODUCTION

Investigations of neuronal models subjected to different types of perturbations have received significant attention in the last years [1-3]. It is widely acknowledged that signal processing in neural systems takes place in a noisy environment. Hence, it is of interest to understand the statistical properties of stochastic neuronal systems. Investigation of the influence of noise on spike generation in the presence of some external forcing signals is particularly important because noise plays a significant role in the detection, transmission, and encoding of such signals [4].

The investigation of multilayer networks is of interest because the networks of brain have a multilayer structure [5-8]. The studies help to understand how the brain works.

Coherence resonance is an important finding emerging in many fields of science, including complex neuronal systems [9-11]. The phenomenon of coherence resonance was first discussed in a simple autonomous system in the vicinity of the saddle-node bifurcation. The nonuniform noise-induced limit cycle leads to a peak at a definite frequency in the power spectrum. The signal-to-noise ratio (SNR) increases first to a maximum and then decreases when the intensity of noise increases, showing the optimization of the coherent limit cycle to the noise.

In this paper, we numerically simulate a two-layer network of coupled Hodgkin-Huxley neurons for modulating a processing visual perception by the human brain [12-16]. The first and the second layers of the network consist of 5 and 50 neurons and represent a visual area of the thalamus and visual cortex respectively. As a model neuron, we chose the Hodgkin-Huxley neuron. We simulate visual stimulus by adding some external stimulus of constant amplitude to the neurons in the first layer connected to the neurons in the second one unidirectionally. We investigate the influence of the external stimulus amplitude on the dynamics of second layer neurons. We calculate power spectra of signal averaged over all neurons in the second layer and then we calculate

signal-to-noise ratio and characteristic correlation time. As a result, we discover coherent resonance phenomenon in the system: there is an area of external stimulus amplitude when both SNR and characteristic correlation time are maximal.

## II. MODEL

The system under study represents the networks of  $N^{\text{ex}}=5$  and  $N=50$  Hodgkin-Huxley neurons (Fig. 1). Inside each network, all elements are connected to each other, and there is a probability  $p=0.3$  of making a one-way connection between a neuron from the first network to a neuron from the second one. To all  $N^{\text{ex}}$  neurons from the first network, we inject the external current  $I^{\text{ex}}$  of constant amplitude simulating the visual stimulus.

The time evolution of the transmembrane potential of each HH neuron is given by

$$C_m \frac{dV}{dt} = -g_{\text{Na}} m^3 h(V - V_{\text{Na}}) - g_K n^4 (V - V_{\text{K}}) - g_L (V - V_{\text{L}}) + I^{\text{ex}} + I^{\text{syn}} \quad (1)$$

where  $C_m = 1\mu\text{F}/\text{cm}^2$  is the capacity of cell membrane,  $I^{\text{ex}}$  is an external bias current injected into a neuron,  $V$  is the membrane potential of a neuron,  $g_{\text{Na}} = 120\text{ mS}/\text{cm}^2$ ,  $g_K = 136\text{ mS}/\text{cm}^2$  and  $g_L = 0.3\text{ mS}/\text{cm}^2$  receptively denote the maximal sodium, potassium and leakage conductance when all ion channels are open.  $V_{\text{Na}} = 50\text{ mV}$ ,  $V_{\text{K}} = -77\text{ mV}$  and  $V_{\text{L}} = -54.4\text{ mV}$  are the reversal potentials for sodium, potassium and leak channels respectively.  $m$ ,  $n$  and  $h$  represent the mean ratios of the open gates of the specific ion channels.  $n^4$  and  $m^3h$  are the mean portions of the open potassium and sodium ion channels within a membrane patch. The dynamics of gating variables ( $x=m,n,h$ ) depending on rate functions  $\alpha_x(V)$  and  $\beta_x(V)$  are given:

$$\frac{dx}{dt} = \alpha_x(V)(1-x) - \beta_x(V)x + \xi_x(t), \quad x = m, n, h \quad (2)$$

$\xi_x(t)$  is independent zero mean Gaussian white noise sources whose autocorrelation functions are given as below

$$\langle \xi_m(t)\xi_m(t') \rangle = \frac{2\alpha_m\beta_m}{N_{\text{Na}}(\alpha_m+\beta_m)} \delta(t-t') \quad (3)$$

$$\langle \xi_h(t)\xi_h(t') \rangle = \frac{2\alpha_h\beta_h}{N_{\text{Na}}(\alpha_h+\beta_h)} \delta(t-t') \quad (4)$$

$$\langle \xi_n(t)\xi_n(t') \rangle = \frac{2\alpha_n\beta_n}{N_K(\alpha_n+\beta_n)} \delta(t-t') \quad (5)$$

where  $N_{\text{Na}}$  and  $N_K$  represent the total number of sodium and potassium channels within a membrane patch, and are calculated as  $N_{\text{Na}} = \rho_{\text{Na}} S$ ,  $N_K = \rho_K S$  where  $\rho_{\text{Na}} = 60\text{ }\mu\text{m}^{-1}$  and  $\rho_K = 18\text{ }\mu\text{m}^{-1}$  are the sodium and potassium channel

densities, respectively.  $S$  is the membrane patch area of each neuron.

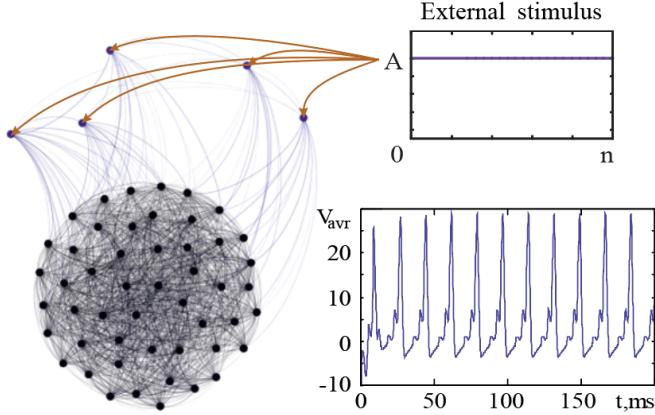


Fig. 1. Network model. The external stimulus with amplitude  $A$  is applied to  $N^{\text{ex}}=5$  neurons in the first network. Each neuron in this network is connected to each neuron in the second network with a probability  $p = 0.3$ . From the system we signal  $V_{\text{avr}}$  averaged over all these neurons. Each element has its own Gaussian noise.

$I_i^{\text{syn}}$  is the total synaptic current received by  $i$ -th neuron. We consider coupling via chemical synapses. The synaptic current takes the form

$$I_i^{\text{syn}} = \sum_{j \in \text{neigh}(i)} g_c e^{-(t-t_0^j)/\tau_{\text{syn}}} (E_{\text{rev}} - V_i) \quad (6)$$

where the alpha function  $\alpha(t)$  describes the temporal evolution of the synaptic conductance,  $g_c$  is the maximal conductance of the synaptic channel,  $t_0^j$  is the time at which presynaptic neuron  $j$  fires,  $\tau_{\text{syn}} = 3 \text{ ms}$ .

### III. RESULTS

We analyze the signal averaged over all  $N$  neurons from the second network  $V_{\text{avr}} = \sum_{i=1}^N V_i / N$ . The example of characteristic neuron dynamics one can on the Fig.1.

To investigate the dynamics of the system we analyze the coherence of a signal. For that, we can calculate the signal-to-noise ratio (SNR) derived from the energy spectrum using the Fourier transform.

The maximum energy in the spectrum  $E_{\text{max}}$  appears at the average frequency of spiking neurons  $f_s$ . Therefore, this spectral component reflects the contribution of regular behavior, while the noise contributes mainly to the background component  $E_N$  at the same frequency  $f_s$ . The signal-to-noise ratio can be calculated from the power spectra as  $\text{SNR} = E_{\text{max}}^2 - E_N^2$  (dB) at the dominant frequency  $f_s$ .

Another way to measure of coherence of the system is the calculation of characteristic correlation time defined as

$$\tau_c = \sum_{n=0}^T C(\tau)^2, \quad (7)$$

where  $t_0$  is the transient time,  $T$  is the total time,  $C(\tau)$  is the autocorrelation function given as

$$C(\tau) = \frac{\langle (x_{\text{avr}}(n) - \langle x_{\text{avr}} \rangle)(x_{\text{avr}}(n+\tau) - \langle x_{\text{avr}} \rangle) \rangle}{\langle (x_{\text{avr}}(n) - \langle x_{\text{avr}} \rangle)^2 \rangle}, \quad (7)$$

where  $\langle \dots \rangle$  is the time average after transients. The larger the correlation time, the better the coherence.

In this work, we calculate the dependencies of signal-to-noise ratio and characteristic correlation time from external stimulus amplitude (Fig. 2). They both have the same

dynamics: at low external stimulus amplitude all neurons are in "silent" regime and there is no spikes generation. Increasing the stimulus amplitude leads to increasing the signal-to-noise ratio and characteristic correlation time. After  $I^{\text{ex}}=10.0 \mu\text{A}/\text{sm}^2$  they start to decrease, so the dependencies have resonance at this amplitude value.

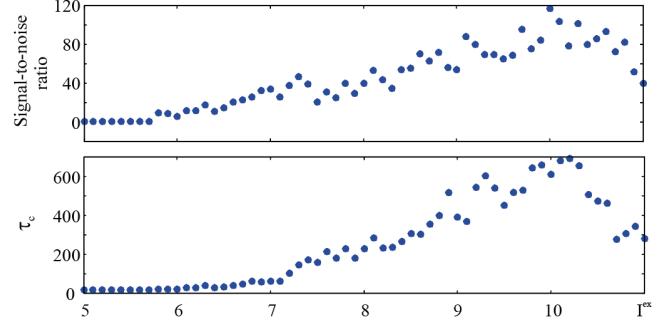


Fig. 2. The dependencies of signal-to-noise ratio and characteristic correlation time from external stimulus amplitude for  $\xi=0.1$ .

### IV. CONCLUSION

We have numerically simulated the dynamics of the brain under visual perception using 2-layer Hodgkin-Huxley neuron network. We have calculated characteristic correlation time and signal-to-noise ratio from power spectra of signal averaging over all neurons in the second layer to measure the coherence of the system. Analyzing the influence of amplitudes of internal noise and external stimulus on system dynamics we found that the coherence is maximal on the certain value of stimulus intensity. It means that the network processes visual information better for some values of external stimulus amplitude.

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