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### Nonlinear correlation method for the separation of couplings in EEG experiments with neural ensembles

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#### ABSTRACT

In the present paper the nonlinear association analysis of the EEG brain data in the process of bistable image perception are realized. Brain functional connectivity can be characterized by the temporal evolution of correlation between signals recorded from spatially-distributed regions. Numerous techniques were introduced for assessing this connectivity. Among nonlinear regression analysis methods, we chose a method introduced in the field of EEG analysis by Pijn, Lopes da Silva and colleagues, based on the fitting of a nonlinear curve by piecewise linear approximation, and more recently evaluated in a model of coupled neuronal populations. This method has some major advantages over other signal analysis methods such as coherence and cross-correlation functions because it can be applied independently of whether the type of relationship between the two signals is linear or nonlinear. In the capacity of bistable image we used a set of images based on a well-known bistable object, the Necker cube, as a visual stimulus. This is a cube with transparent faces and visible ribs. Bistability in perception consists in the interpretation of this 3D-object as to be oriented in two different ways, in particular, if the different ribs of the Necker cube are drawn with different intensity. It was shown that the structure of connections in the brain is different for cases without visual stimulation and with stimulation with the help of the Necker cube.

Keywords: Multistablity, nonlinear control, numerical methods, electroencephalogram.

#### 1. INTRODUCTION

Nowadays, the study of brain dynamics in cognitive activity attracted much attention of researchers.<sup>1–3</sup> Such studies often used electroencephalography, because this method is non-invasive and does not require significant limitations volunteer mobility, nor for costs.<sup>4,5</sup> The use of mathematical methods for the analysis of EEG is gaining popularity, including methods of nonlinear dynamics.<sup>6,7</sup>

The investigations of nonlinear processes in the brain neural network during perception of ambiguous (the so-called bi- and multistable) images are very important for the understanding of both the visual recognition of objects and the decision-making process. Nowadays, the perception of ambiguous images attracts huge attention of many scientists. In a sense, such images are good objects for studying the visual perception in general as well as the decision-making mechanisms. Images of this type have been the object of research for psychologists for a long time.<sup>4,8</sup> Recently, ambiguous images awoke interest of physicists and mathematicians.<sup>9,10</sup> Despite of considerable efforts of many researchers, the main mechanisms underlying interpretation of a multistable image are not well understood. At present, perception is known to be a result of nonlinear processes which take place in the distributed neural network of occipital, parietal and frontal regions of the brain cortex.<sup>8,11</sup> The perception of ambiguous (bistable) images was thoroughly investigated in the last decade. The most popular bistable images are Rubin vase, Mach bands, Rorschach test, Boring's old/young woman illusion, Necker cube, etc.<sup>5,12-14</sup>

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In this work for study of brain dynamics in cognitive activity the brain structures are analyzed on their functional connectivity in order to reveal the dynamics of detailed network. Functional connectivity between brain structures was studied with the aid of the non-linear association analysis. <sup>15</sup> This signal analytical technique has frequently been shown to be a reliable measure for functional coupling of brain signals. Its main advantage above several other connectivity measures is that it does not presume a linear relationship between signals and is able to reveal information about the direction of coupling. It is a time-domain analysis, which can reveal three different parameters of interest: the strength of functional coupling or maximal association between two brain signals  $h^2$ ; time-delays of a signal between brain structures or signal transduction time  $\tau$ ; the direction of functional coupling.

#### 2. EXPERIMENT

Unsymmetrical Necker cube was used as ambiguous image in our experiments. The contrast of the three middle lines centered in the left middle corner was used as one of the control parameter I taking the values from the range [0; 1]. If I is equal to 1 observer will see the right-oriented cube, whereas zero value of the control parameter corresponds to the left-oriented cube. The intensity of the three middle lines centered in the right corner was set to (1 - I), and the intensity of the six visible outer cube edges was fixed to 1. For another values of control parameter there will be spontaneous alternations between these two projections of Necker cube in the process of its visual perception. Similar experiments are described in the works. <sup>16, 17</sup>

Necker cube image was placed in the middle of the computer screen on the wight background. The bistable visual perception of the Necker cube image was explained to and really seen by all participants. Subjects were instructed to press left or right keys on the control panel each time their perception of the cube changed. The experiment consists of several runs of 10 min each. The runs were interrupted by breaks of a lengths freely chosen by the subjects, thus minimizing tiring effects. <sup>18,19</sup> The duration of each period at constant perception was computed from the time interval between two successive keystrokes. Total time of experiment was about 50 minutes for each cube. To organize visual stimulation and data registration an equipment of Medicom MTD "ENCEPHALAN EEGR-19/26" with corresponding software program was used. Sampling frequency of EEG was equal to 250 Hz, frequency range of data was from 0.016 Hz to 70 Hz with a notch filter at 50 Hz. For EEG registration monopolar method of registration and the standard international system "10-20" for placing electrodes were used. <sup>20</sup>

#### 3. METHOD

To estimate the degree of association between two signals and the corresponding time delay, the nonlinear correlation coefficient  $h^2$  was calculated as a function of time shift  $(\tau)$  between the two signals. This statistical measure was first introduced in EEG signal analysis by Pijn and colleagues.<sup>15,21</sup> It describes the dependency of a signal Y on a signal X in a general way. This method has some major advantages over other signal analysis methods such as coherence and cross-correlation functions because it can be applied independently of whether the type of relationship between the two signals is linear or nonlinear. Details of the theoretical and practical aspects of this method can be found in the above-mentioned reports. The basic idea is that if the amplitude of signal Y is considered as a function of the amplitude of signal X, the value of y given a certain value of x can be predicted according to a nonlinear regression curve. The variance of Y according to the regression curve is called the explained variance, i.e., it is explained or predicted on the basis of X. By subtracting the explained variance from the total variance one obtains the unexplained variance. The correlation ratio  $\eta^2$  expresses the reduction of variance of Y that can be obtained by predicting the y values according to the regression curve as follows:  $\eta^2$  (total variance - unexplained variance)/total variance.

In practice, a numerical approximation of the nonlinear regression curve is obtained by describing the scatterplot of y versus x by segments of linear regression curves. The variable x is subdivided into bins; for each bin the x value of the midpoint  $(p_i)$  and the average value of y  $(q_i)$  are calculated, and the resulting points  $(p_i, q_i)$  are connected by segments of straight lines (= linear regression curves). The nonlinear correlation coefficient  $h^2$ , which is the estimator for  $\eta^2$ , can now be computed as the fraction of total variance that can be explained by the segments of linear regression lines, as follows:

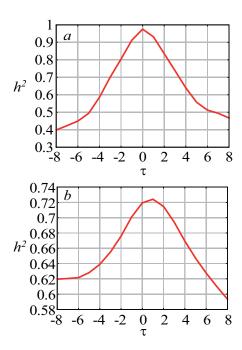


Figure 1. The dependence of nonlinear correlation coefficient  $h^2$  on the time shift  $(\tau)$  for example for O2-P4 (a) and P3-Pz (b) channels

$$h^{2} = \frac{\sum_{i=1}^{N} (y_{i} - \langle y \rangle)^{2} - \sum_{i=1}^{N} (y_{i} - f(x_{i}))^{2}}{\sum_{i=1}^{N} (y_{i} - \langle y \rangle)^{2}}$$
(1)

with N being the number of samples and  $\langle y \rangle$  being the average of all  $y_i$ . The estimator  $h_2$ , which signifies the strength of the association between the two signals, can take values between 0 (Y is totally independent of X) and 1 (Y is completely determined by X). In the case of a linear relationship between x and y, the  $\eta^2$  reduces to the common regression coefficient  $r^2$ . Similarly, as in the case of the cross-correlation, one can estimate  $h^2$  as a function of time shift ( $\tau$ ) between signal X and Y or vice versa. That shift for which the maximum value for  $h^2$  is reached is used as an estimate of the time lag between the two signals.

In figure 1 the application of the method of nonlinear correlations for the analysis of EEG data of the brain are shown. As an example, we are show the case with a time-shift and without. On the figure 1a of the maximum value the correlation coefficient reaches for time shift  $\tau = 0$ . The value of the correlation coefficient is close to 1. In this case, we say that the time delay is not observed. On the figure 1b, opposite, it can be seen that the maximum value of the correlation coefficient corresponds to a time shift  $\tau = 1$ . The value of the correlation coefficient is less than in the previous case. In this case, a time delay of 1 is observed.

#### 4. RESULT

In this paper consider how change the pattern of connections in the brain with visual stimulation by nonlinear associations analyzing of the EEG data. For this investigation, we consider cases without visual stimulation and with stimulation with use of the Necker cube with different intensities of internal facets. The order of the experiment and the method of nonlinear associations are described in the previous sections.

With visual stimulation, the most important are the connections in the occipital region of the brain where visual images are processed. In figure 2 shown associations in the occipital region without visual stimulation and in the presence of a visual stimulus. It can be seen that the connection between the O2-P4 channels is constant, however, when stimulating the image of the Necker cube, a large number of other connections appear in the occipital region. For different intensities of internal faces of Necker cube connections are different, but for all of

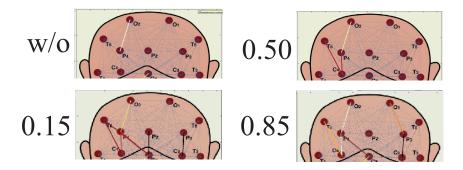


Figure 2. Strength of association in the occipital region of the brain by the analysis of EEG data with use of the method of nonlinear associations. The lighter the line, the higher the value of the correlation coefficient. The associations are shown for case without of visual stimulation and for stimulation with Necker cubes with different intensities of internal faces (the values of parameter I are notice near with the images))

them we see connections T6-C4 and P4-C4. Thus, it can be seen that the connections depend on the presence of visual stimulation and the perception of the Necker cube. Thus, for intensity I = 0.15, the perception of the cube as the left one is more probable, for I = 0.85 as the right one, for I = 0.50 both probabilities of the cube are equally probable.

Equally important for a full and fundamental investigation of the connections in the brain is the consideration of different frequency ranges. It is known that in different frequency ranges, some effects of the analysis of brain function are appeared in different ways. Or they can only appear in a certain frequency range. Therefore, we were considered four frequency bands:  $\delta$ -rithm rhythm (1-4 Gz),  $\theta$ -rithm rhythm (4-7 Gz),  $\alpha$ -rithm rhythm (8-14 Gz),  $\beta$ -rithm rhythm (14-30 Gz). For all these frequency ranges, the configurations of the brain connections were constructed, as in figure 2. They are shown in figure 3. It can be seen that for all frequency bands there are both an abode structure (often a triangle O2-T6-P4) and various for cases when there is no visual stimulation and when it is present. The connections for different intensities of the inner faces of the Necker cube are slightly different for one frequency band. Between the different frequency ranges, the differences are obvious. In the case where visual stimulation is absent, often there are connections in the left hemisphere: O1-P3 and / or T5-P3.

#### 5. CONCLUSION

In the present paper are investigation the connection in brain with use of the nonlinear association analysis of the EEG brain data in the process of bistable image perception. The special attention has the differences between cases without visual stimulation and visual stimulation with the help of the Necker cube with different intensity of internal facets. It was shown that the structure of connections in the brain is different for these cases when considering the occipital part. For different frequency ranges, it was shown that the connections in the left hemisphere are more characteristic for the case without visual stimulation, whereas the connections in the right hemisphere almost coincide for both cases. These effects, observed in the brain, can be used for a in-depth study of the process of image perception.

#### 6. ACKNOWLEDGMENTS

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#### REFERENCES

- [1] Hramov A.E., Koronovskii A.A., Kurovskaya M.K., Ovchinnikov A.A., Boccaletti S., "Length distribution of laminar phases for type- I intermittency in the presence of noise" *Phys. Rev. E.* **76** (2), 026206 (2007).
- [2] van Luijtelaar, G., Lttjohann, A., Makarov, V. V., Maksimenko, V. A., Koronovskii, A. A., and Hramov, A. E., "Macroscopic and microscopic spectral properties of brain networks during local and global synchronization," *Phys. Rev. E.* 96, 012316 (2017).

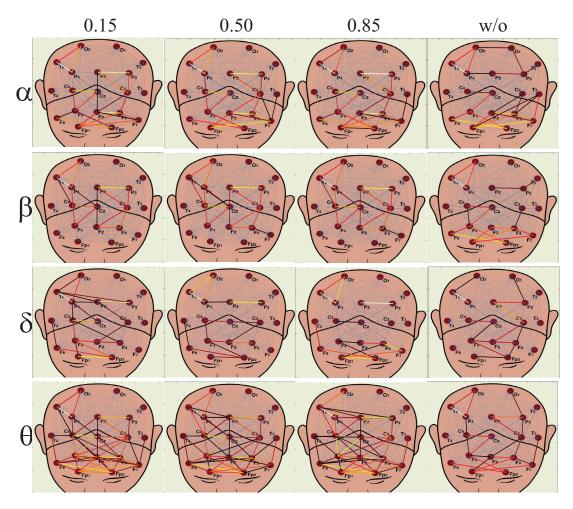


Figure 3. Strength of association for different frequency range of the brain by the analysis of EEG data with use of the method of nonlinear associations. The lighter the line, the higher the value of the correlation coefficient. The values of parameter I are notice from top (w/o - case without of visual stimulation), the frequency range are notice from left

- [3] Maksimenko V.A., Heukelum S., Makarov V.V., Kelderhuis J., Luttjohann A., Koronovskii A.A., Hramov A.E., van Luijtelaar G., "Absence Seizure Control by a Brain Computer Interface," *Scientific Reports* 7 (2487), 1-8 (2017).
- [4] Niedermeyer, E., da Silva, F. L., [Electroencephalography: Basic Principles, Clinical Applications, and Related Fields], Lippincot, Williams and Wilkins (2004).
- [5] Sitnikova, E., Hramov, A. E., Koronovskii, A. A., and van Luijtelaar, G., "Sleep spindles and spikewave discharges in EEG: Their generic features, similarities and distinctions disclosed with Fourier transform and continuous wavelet analysis," *Journal of Neuroscience Methods* 180, 304-316 (2009).
- [6] Sitnikova E.Yu., Hramov A.E., Grubov V.V., Ovchinnikov A.A., Koronovskii A.A., "Onoff intermittency of thalamo-cortical oscillations in the electroencephalogram of rats with genetic predisposition to absence epilepsy" *Brain research.* **1436**, 147-156 (2012).
- [7] Sitnikova E.Yu., Hramov A.E., Grubov V.V., Koronovskii A.A., "Time-frequency characteristics and dynamics of sleepspindles in WAG/Rij rats with absence epilepsy," *Proc. of SPIE* **1543**, 290-299 (2014).
- [8] Buzsaki, G., and Draguhn, A., "Neuronal oscillations in cortical networks," Science 304, 19261929 (2004).
- [9] van Luijtelaar, G., Hramov, A. E., Sitnikova, E. Yu., and Koronovskii, A. A., "Spike-wave discharges in WAG/Rij rats are preceded by delta and theta precursor activity in cortex and thalamus," *Clinical Neurophysiology* **122**, 687-695 (2011).

- [10] van Luijtelaar, G., Luttjohann, A., Makarov, V. V., Maksimenko, V. A., Koronovskii, A. A., and Hramov, A. E., "Methods of automated absence seizure detection, interference bystimulation, and possibilities for prediction in genetic absence models," *Journal of Neuroscience Methods* 260, 144-158 (2016).
- [11] Nazimov, A. I., Pavlov, A. S., Nazimova, A. A., Grubov, V. V., Koronovskii, A. A., Sitnikova, E. Yu., Hramov, A. E., "Serial identification of EEG patterns using adaptive wavelet-based analysis" Eur. Phys. J. Special Topics 222, 2713-2722 (2013).
- [12] Doron, I., Hulata, E., Baruchi, I., Towle, V. L., Ben-Jacob E., "Time-Invariant Person-Specific Frequency Templates in Human Brain Activity," *Physical Review Letters* **96**, 258101 (2006).
- [13] Hramov, A. E., Koronovskii, A. A., Makarov, V. A., Pavlov, A. N., and Sitnikova, E. Y., [Wavelets in Neuroscience], Heidelberg New York Dordrecht London (2015).
- [14] van Vugt, M. K., Sederberg, P. B., Kahana, M. J., "Comparison of spectral analysis methods for characterizing brain oscillations," *Journal of Neuroscience Methods* **162**, 49-63 (2007).
- [15] Pijn JPM, Vijn PCM, Lopes da Silva FH, Van Emde Boas W, Blanes W, "The use of signal-analysis for the localization of an epileptogenic focus: a new approach," *Adv Epileptology* 17, 272-276 (1989).
- [16] Hramov A.E., Maksimenko V.A., Pchelintseva S.V., Runnova A.E., Grubov V.V., Musatov V.Yu., Zhuravlev M.O., Koronovskii A.A., Pisarchik A.N., "Classifying the perceptual interpretations of a bistable image using EEG and artificial neural networks," Frontiers in neuroscience 11, 674 (2017).
- [17] Runnova A.E., Hramov A.E., Grubov V.V., Koronovskii A.A., Kurovskaya M.K., Pisarchik A.N., "Theoretical background and experimental measurements of human brain noise intensity in perception of ambiguous images" *Chaos, Solitons and Fractals* **93**, 201-206 (2016).
- [18] Grubov, V. V., Runnova, A. E., Kurovskaya, M. K., Pavlov, A. N., Koronovskii, A. A., and Hramov, A. E., "Demonstration of brain noise on human EEG signals in perception of bistable images," *Proc. SPIE* 9707, 970702 (2016).
- [19] Merk, I., and Schnakenberg, J., "A stochastic model of multistable visual perception" *Biological Cybernetics* 86, 111-116 (2002).
- [20] Jasper, H. H., "The ten-twenty electrode system of the International Federation," Electroencephalogr Clin Neurophysiol 10, 371-375 (1958).
- [21] Lopes da Silva FH, Pijn JP, Boeijinga P., "Interdependence of EEG signals: linear vs. nonlinear associations and the significance of time delays and phase shifts," *Brain Topogr* **2**(9), 18 (1989).